# **Data Wrangling and Data Analysis**

# **Data Extraction**

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#### Outlines

- So Far
  - Data types
    - Structured, semi-structured and unstructured
  - Data Models
    - Relational model and entity-relationship model
    - Graphs and trees
    - Objects
  - Data model components
    - Data, structure, semantics, and operations
  - Databases vs file systems
  - DDL and DML
  - Creating and modifying tables (relations) in SQL



#### Outlines

- Today
  - Operations on databases
    - Relational algebra
    - SQL



# Reading Material for Today

Database System Concepts (7<sup>th</sup> Edition) CH 2.6, 3.3 – 3.8.

# Abraham Silbers chatt Borny K Korth S Sudarshan

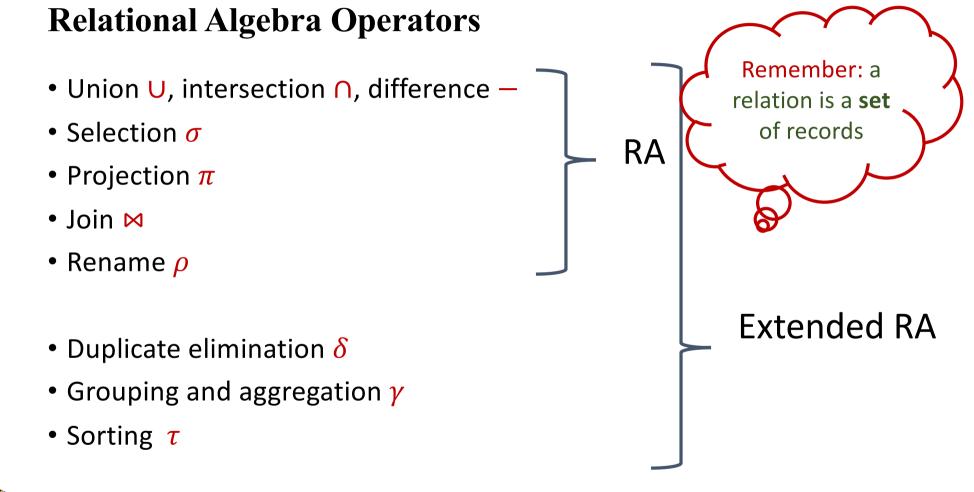
**Database System Concepts** 

SEVENTH EDITION



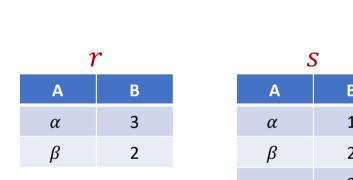
**Relational Algebra** 







#### Union



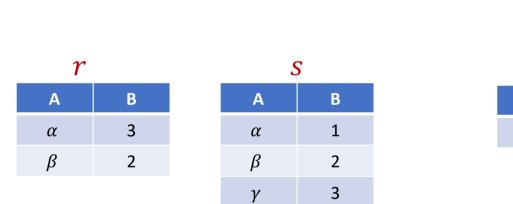
| S |   |  |  |
|---|---|--|--|
| Α | В |  |  |
| α | 1 |  |  |
| β | 2 |  |  |
| γ | 3 |  |  |

| $r \cup s$ |   |  |
|------------|---|--|
| Α          | В |  |
| α          | 1 |  |
| β          | 2 |  |
| γ          | 3 |  |
| α          | 3 |  |



r U s

#### Intersection

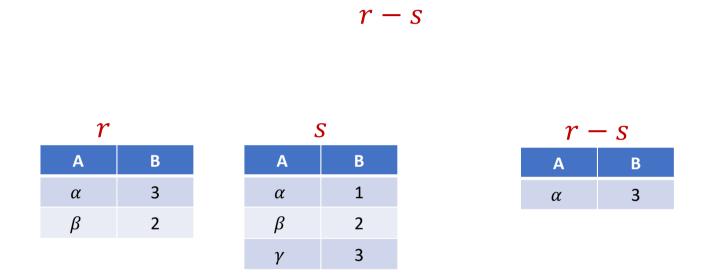


 $r \cap s$ 





#### Difference



Can you find an expression that is equivalent to r - s using the operators  $\cap$  and  $\sim$ ?



#### Selection

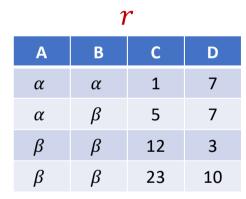
| r |   |    |    |  |
|---|---|----|----|--|
| Α | В | С  | D  |  |
| α | α | 1  | 7  |  |
| α | β | 5  | 7  |  |
| β | β | 12 | 3  |  |
| β | β | 23 | 10 |  |

| $\sigma_{(A=B) \land (D>5)}$ | ( <i>r</i> ) |
|------------------------------|--------------|
|------------------------------|--------------|

| Α | В | С  | D  |
|---|---|----|----|
| α | α | 1  | 7  |
| β | β | 23 | 10 |



### Projection





| Α | С  |
|---|----|
| α | 1  |
| α | 5  |
| β | 12 |
| β | 23 |



#### Join

#### **Cartesian Product**

| r |   | 2 | S |
|---|---|---|---|
| Α | В | С | D |
| α | 3 | α | 1 |
| β | 2 | β | 2 |
|   |   | γ | 3 |

 $r \times s$ 

| Α | В | С | D |
|---|---|---|---|
| α | 3 | α | 1 |
| α | 3 | β | 2 |
| α | 3 | γ | 3 |
| β | 2 | α | 1 |
| β | 2 | β | 2 |
| β | 2 | γ | 3 |
|   |   |   |   |



#### Join

#### **Cartesian Product**

| r |   |   | S |
|---|---|---|---|
| Α | В | А | С |
| α | 3 | α | 1 |
| β | 2 | β | 2 |
|   |   | γ | 3 |

 $r \times s$ 

| r.A | В | s.A | С |  |
|-----|---|-----|---|--|
| α   | 3 | α   | 1 |  |
| α   | 3 | β   | 2 |  |
| α   | 3 | γ   | 3 |  |
| β   | 2 | α   | 1 |  |
| β   | 2 | β   | 2 |  |
| β   | 2 | γ   | 3 |  |
|     |   |     |   |  |



#### Rename

Rename operation  $\rho_x(E)$  returns the output of the expression E under the name x

| r |  |  |
|---|--|--|
| В |  |  |
| 3 |  |  |
| 2 |  |  |
|   |  |  |

| $r \times \rho_s(r)$ |     |     |     |  |
|----------------------|-----|-----|-----|--|
| r.A                  | r.B | s.A | s.B |  |
| α                    | 3   | α   | 3   |  |
| α                    | 3   | β   | 2   |  |
| β                    | 2   | α   | 3   |  |
| β                    | 2   | β   | 2   |  |

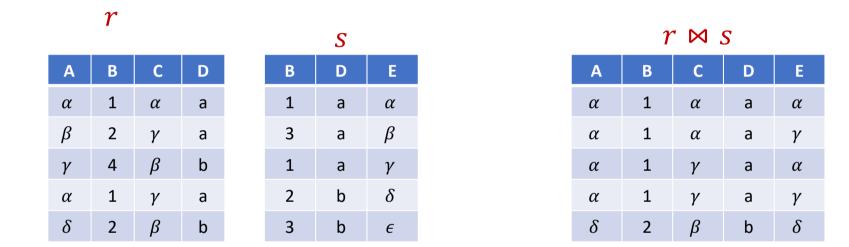


#### **Natural Join**

- Let r and s be relations on schemas R and S, respectively.
- Natural join of relations R and S is a relation on schema R ∪ S obtained as follows:
  - Consider each pair of tuples  $t_r$  from r and  $t_s$  from s.
  - If t<sub>r</sub> and t<sub>s</sub> have the same value on each of the attributes in R ∩ S, add a tuple t to the result, where
    - t has the same value as  $t_r$  on r
    - t has the same value as  $t_s$  on s



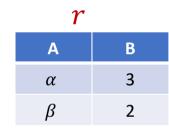
#### **Natural Join – Example**

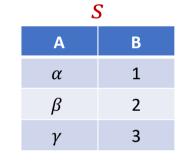


 $r \bowtie s \equiv \pi_{A,r.B,C,r.D,E}(\sigma_{r.B=s.B \land r.D=s.D}(r \times s))$ 



#### **Composition of Operations**





| $r \times s$ |     |     |     |  |
|--------------|-----|-----|-----|--|
| r.A          | r.B | s.A | s.B |  |
| α            | 3   | α   | 1   |  |
| α            | 3   | β   | 2   |  |
| α            | 3   | γ   | 3   |  |
| β            | 2   | α   | 1   |  |
| β            | 2   | β   | 2   |  |
| β            | 2   | γ   | 3   |  |



| r.A | r.B | s.A | s.B |
|-----|-----|-----|-----|
| α   | 3   | α   | 1   |
| β   | 2   | β   | 2   |



#### **Summary of Relational Algebra Operators**

| Symbol (name)            | Description  |
|--------------------------|--|
| $\sigma$ (Selection)     | Return rows of the input relation that satisfy a predicate.  |
| $\pi$ (Projection)       | Return specified attributes from all rows of the input relation.<br>Remove duplicate tuples from the output.                 |
| × (Cartesian<br>Product) | Return pairs of rows from the <i>two</i> input relations.  |
| U (Union)                | Return the union of tuples from the <i>two</i> input relations.  |
| – (Difference)           | Return the set of records that exist in the relation before the operator(-) but not in the relation after the operator.      |
| $\cap$ (Intersection)    | Return the common tuples in both input relations.  |
| ⋈ (Natural Join)         | Return pairs of rows from the <i>two</i> input relations that have the same value on all attributes that have the same name. |
| $\rho$ (Rename)          | Returns the outcome of an expression under the specified name  |
| echt University          |  |

#### **Remarks on RA**

- Each Query input is a table (or set of tables)
- Each query output is a table.
- All data in the output table appears in one of the input tables
- Can we compute:
  - SUM  $\gamma_{SUM(tot\_credit)}(student)$
  - AVG  $\gamma_{AVG(salary)}(instructor)$
  - MAX  $\gamma_{MAX(buget)}(department)$
  - MIN  $\gamma_{MIN(budget)}(department)$
  - COUNT  $\gamma_{COUNT(tot\_credit \ge 12)}(student)$
  - **GROUP BY** dept\_name  $\gamma_{AVG(salary)}(instructor)$



Data Extraction Using Structured Query Language (SQL)



#### **SELECT-FROM-WHERE Statements**

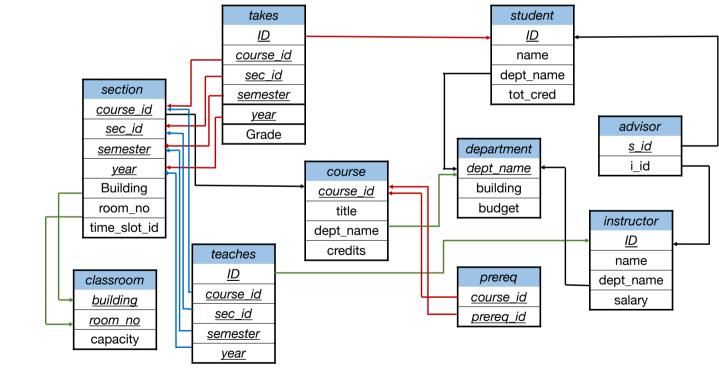
SELECT desired attributes

FROM one or more tables

WHERE condition about tuples of the tables



# Remember Our Main Database?





#### **Example: The SELECT Clause**

• Get the IDs, names and total credits of students who completed at least 24 credits

```
SELECT ID, name, tot_cred
FROM student
WHERE tot_cred >= 24;
```

- The answer is a relation with three attributes (ID, name, tot\_cred)
- What if we need only the names of the students?
- Note that: the SQL operator names are case insensitive SELECT  $\equiv$  Select  $\equiv$  select



### **The SELECT Clause**

- Lists the desired attributes in the result of the query
  - Corresponds to the projection operator of the relational algebra
- SQL allows duplicates in relations as well as in query results
- To force the elimination of duplicates, use the keyword **DISTINCT** after select
- Example: find the department names of all instructors whose salary is strictly greater than 60000 without showing the department name more than once

SELECT DISTINCT dept\_name FROM instructor WHERE salary > 60000



#### The SELECT Clause (Cont.)

• The keyword **ALL** specifies that duplicates should not be removed

SELECT ALL dept\_name FROM instructor WHERE salary > 60000

 An asterisk in the SELECT clause denotes "all attributes" SELECT \* FROM instructor will return all the records from table "instructor"



# **The SELECT Clause (Cont.)**

• An attribute could be literal with no **FROM** clause SELECT '542'

Results in a relation with one column and one row with value "542'

We can also give the column a name using

SELECT '542' AS V1

• An attribute could be a literal with **FROM** clause

SELECT 'A' FROM instructor

will return a relation with one column and N rows (the number of tuples in the 'instructor ' relation) where each row will contain the value "A"



### **The SELECT Clause (Cont.)**

 SELECT clause can contain arithmetic expressions involving the operations \*, +, -, and /.

SELECT ID, name, salary/12.0

**FROM** instructor

This query would return a relation with the same number of records as the 'instructor' relation and the (ID, name, salary/12.0) where the yearly salary is replaced by the monthly salary

We can rename the "salary/12.0" using the **AS** clause

SELECT ID, name, salary/12.0 as monthly\_salary

**FROM** instructor



### **The WHERE Clause**

- Specifies conditions that the result must satisfy
  - Corresponds to the selection predicate of the relational algebra
- To find all students enrolled in the 'Math.' department SELECT ID, name FROM student WHERE dept\_name = 'Math.'
- Conditions can be also combined using logical operators (AND, OR, NOT)
  - Find all students in the 'Math.' department who completed a minimum of 24 credits SELECT ID, name FROM student

WHERE dept\_name = 'Math.' AND tot\_cred >= 24

• Comparisons =, <>, <, >, <=, >=



### The FROM Clause

- Lists the relations involved in the query
  - Corresponds to the Cartesian product operation of the relational algebra
- Find the Cartesian product 'instructor' X' teaches'

#### SELECT \* FROM instructor, teaches

- Generates every possible instructor teaches pair, with all attributes from both relations.
- For common attributes (e.g., *ID*), the attributes in the resulting table are renamed using the relation name (e.g., *instructor.ID*)
- Similar to the cartesian product in RA
- Cartesian product not very useful directly, but useful when combined with where-clause condition.



#### **SELECT-FROM-WHERE Examples**

SELECT name, course\_id

FROM instructor, teaches

WHERE instructor.ID = teaches.ID

Returns the names of all instructors who have taught any courses and the course\_id

SELECT name, course\_id

FROM instructor, teaches

WHERE instructor.ID = teaches.ID AND instructor.dept\_name = 'Art'

Returns the names of all instructors in the Art department who have taught any courses and the course\_id



#### **The Rename Operation**

• SQL allows renaming relations and attributes using the **AS** clause:

#### old-name AS new-name

• Find the names of all instructors who have a higher salary than some instructor in 'Comp. Sci'.

SELECT DISTINCT T.name

FROM instructor AS T, instructor AS S

WHERE T.salary >= 75000 AND S.dept\_name = 'Comp. Sci.'

Returns the names of instructors in the 'Comp. Sci.' department joined with whose salary is greater than or equal 75000

 Keyword AS is optional and may be omitted instructor AS T = instructor T



#### **Renaming Example: Self-Join**

- Sometimes, a query needs to use two copies of the same relation.
- Distinguish copies by renaming the relations.
- Example self-Join

SELECT T.name AS N1, S.name AS N2 FROM instructor T, instructor S WHERE T.salary = S.salary AND T.name < S.name

- Returns the names of instructors who has the same salary
- Do not produce pairs like (Miller, Miller)
- Produces pairs in alphabetic order, e.g. (Adison, Miller), not (Miller, Adison)
- Note that we omit AS when renaming the relations



# **Join Operation**

- JOIN operations take two relations and return as a result another relation.
- A join operation is a Cartesian product which requires that tuples in the two relations match (under some condition). It also specifies the attributes that are present in the result of the join
- The join operations are typically used as subquery expressions in the **FROM** clause



### Join Operation (Cont.)

- We will consider the following relations in the few coming slides
- Relation *course*

| course_id | title           | dept_name  | credits |
|-----------|-----------------|------------|---------|
| BIO-301   | Genetics        | Biology    | 4       |
| CS-490    | Game Design     | Comp. Sci. | 4       |
| CS-315    | Boolean Algebra | Comp. Sci. | 3       |

• Relation prereq

| course_id | prereq_id |
|-----------|-----------|
| BIO-301   | BIO-101   |
| CS-490    | CS-101    |
| CS-347    | CS-201    |



- Note that:
  - *prereq* information is missing for course CS-315
  - course information is missing for course CS-347

#### **Outer Join**

- An extension of the join operation that avoids loss of information.
- Computes the join and then adds tuples form one relation that does not match tuples in the other relation to the result of the join.
- Uses null values.



#### **Left Outer Join**

SELECT \* FROM *course* LEFT OUTER JOIN prereq ON course.course\_id = prereq.course\_id

| course_id | title           | dept_name  | credits | prereq_id |
|-----------|-----------------|------------|---------|-----------|
| BIO-301   | Genetics        | Biology    | 4       | BIO-101   |
| CS-490    | Game Design     | Comp. Sci. | 4       | CS-101    |
| CS-315    | Boolean Algebra | Comp. Sci. | 3       | null      |



# **Right Outer Join**

SELECT \* FROM *course* RIGHT OUTER JOIN prereq

# ON course.course\_id = prereq.course\_id

| course_id | prereq_id | title       | dept_name  | credits |
|-----------|-----------|-------------|------------|---------|
| BIO-301   | BIO-101   | Genetics    | Biology    | 4       |
| CS-490    | CS-101    | Game Design | Comp. Sci. | 4       |
| CS-347    | CS-201    | null        | null       | null    |

- Remember:
  - The order of the attributes in a relation has no meaning



#### **Full Outer Join**

SELECT \* FROM *course* 

#### FULL OUTER JOIN prereq

ON course.course\_id = prereq.course\_id

| course_id | prereq_id | title           | dept_name  | credits |
|-----------|-----------|-----------------|------------|---------|
| BIO-301   | BIO-101   | Genetics        | Biology    | 4       |
| CS-490    | CS-101    | Game Design     | Comp. Sci. | 4       |
| CS-347    | CS-201    | null            | null       | null    |
| CS-315    | null      | Boolean Algebra | Comp. Sci. | 3       |



### **Inner Join**

SELECT \* FROM *course* 

INNER JOIN prereq

ON course.course\_id = prereq.course\_id

| course_id | prereq_id | title       | dept_name  | credits |
|-----------|-----------|-------------|------------|---------|
| BIO-301   | BIO-101   | Genetics    | Biology    | 4       |
| CS-490    | CS-101    | Game Design | Comp. Sci. | 4       |

- An SQL INNER JOIN is same as JOIN clause
- Question:
  - What is the difference between the above JOIN and the right/left outer join



# **String Operations**

- SQL includes a string-matching operator for comparisons on character strings.
- The operator LIKE uses patterns that are described using two special characters
  - Percent (%). The % character matches any substring.
  - Underscore ( \_ ). The \_ character matches any character.
- Example: find the names of all instructors whose name includes the substring "Van der"

SELECT DISTINCT *name* FROM *instructor* WHERE *name* LIKE '%Van der%'



# **String Operations (Cont.)**

• Match the string "100%"

```
LIKE '100 \' ESCAPE '\'
```

in that above we use backslash (\) as the escape character

- Patterns are case sensitive.
- Pattern matching examples:
  - 'Intro%' matches any string beginning with "Intro".
  - '%Comp%' matches any string containing "Comp" as a substring.
  - '\_\_\_' matches any string of exactly three characters.
  - '\_\_\_%' matches any string of at least three characters.



# **Range Queries**

- SQL includes a **BETWEEN** comparison operator
- Example: Find the names of all instructors with salary between \$90,000 and \$100,000 (that is,  $\ge$  \$90,000 and  $\le$  \$100,000)

SELECT *name* FROM *instructor* WHERE *salary* BETWEEN 90000 AND 100000



#### **Tuple Comparison**

SELECT name, course\_id FROM instructor, teaches WHERE (instructor.ID, dept\_name) = (teaches.ID, 'Biology')



#### **Set Operations**

 Find courses that ran in Fall 2009 or in Spring 2010 SELECT course\_id FROM section WHERE sem = 'Fall' AND year = 2009 UNION

SELECT course\_id FROM section WHERE sem = 'Spring' AND year = 2010

 Find courses that ran in Fall 2009 and in Spring 2010 SELECT course\_id FROM section WHERE sem = 'Fall' AND year = 2009 INTERSECT

SELECT course\_id FROM section WHERE sem = 'Spring' AND year = 2010

 Find courses that ran in Fall 2009 but not in Spring 2010 SELECT course\_id FROM section WHERE sem = 'Fall' AND year = 2009 EXCEPT

SELECT course\_id FROM section WHERE sem = 'Spring' AND year = 2010



### **Null Values**

- It is possible for tuples to have a null value, denoted by NULL, for some of their attributes
- *null* signifies an unknown value or that a value does not exist.
- The result of any arithmetic expression involving *NULL* is *NULL* 
  - Example: 5 + *NULL* returns NULL
- The predicate IS NULL can be used to check for null values.
  - Example: Find all instructors whose salary is null.

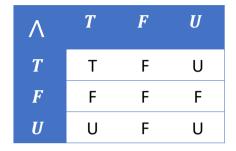
SELECT name FROM instructor WHERE salary IS NULL

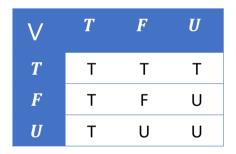


# **Null Values and Three Valued Logic**

- Three values true, false, unknown
- Any comparison with *null* returns *unknown* 
  - Example: 5 < null or null <> null or null = null
- Three-valued logic using the value *unknown*:
  - OR: (unknown OR true) = true, (unknown OR false) = unknown (unknown OR unknown) = unknown
  - AND: (true AND unknown) = unknown, (false AND unknown) = false, (unknown AND unknown) = unknown
  - NOT: (NOT unknown) = unknown
  - "P is unknown" evaluates to true if predicate P evaluates to unknown
- Result of **WHERE** clause predicate is treated as *false* if it evaluates to *unknown*







# **The IN Operator**

- <v> IN <S> evaluates to true if the value v matches one of the values in S.
- It can be used to replace a sequence of conditions connected by **OR**
- Example:

```
SELECT name
FROM instructor
WHERE dept_name IN ('Comp. Sci.', 'Math.', 'Chem.');
```

This Query is equivalent to:

```
SELECT name
FROM instructor
WHERE dept_name = 'Comp. Sci.' OR dept_name = 'Math.' OR dept_name =
'Chem.'
```



#### **Aggregate Functions**

• These functions operate on the multiset of values of a column of a relation, and return a value

avg: average valuemin: minimum valuemax: maximum valuesum: sum of valuescount: number of values



### **Aggregate Functions (Cont.)**

Find the average salary of instructors in the Computer Science department

```
SELECT AVG (salary)
FROM instructor
WHERE dept_name= 'Comp. Sci.';
```

• Find the total number of instructors who taught a course in the Spring 2010 semester

```
SELECT COUNT (DISTINCT ID)
FROM teaches
WHERE semester = 'Spring' AND year = 2010;
```

• Find the number of tuples in the *course* relation

```
SELECT COUNT (*)
FROM course;
```



#### **Aggregate Functions (Cont.)**

 Find the average salary of instructors in each department SELECT dept\_name, AVG (salary) AS avg\_salary FROM instructor GROUP BY dept\_name;

| 22322       Einstein       Physics       95000         33452       Gold       Physics       87000         21212       Wu       Finance       90000         10101       Brandt       Comp. Sci.       82000         43521       Katz       Comp. Sci.       75000         98531       Kim       Biology       78000         58763       Crick       Elec. Eng.       80000         52187       Mozart       History       65000 |   | ID    | name     | dept_name  | salary |
|--|---|-------|----------|------------|--------|
| 21212       Wu       Finance       90000         10101       Brandt       Comp. Sci.       82000         43521       Katz       Comp. Sci.       75000         98531       Kim       Biology       78000         58763       Crick       Elec. Eng.       80000         52187       Mozart       History       65000         32343       El Said       History       86000   |   | 22322 | Einstein | Physics    | 95000  |
| 10101       Brandt       Comp. Sci.       82000         43521       Katz       Comp. Sci.       75000         98531       Kim       Biology       78000         58763       Crick       Elec. Eng.       80000         52187       Mozart       History       65000         32343       El Said       History       86000  |   | 33452 | Gold     | Physics    | 87000  |
| 43521       Katz       Comp. Sci.       75000         98531       Kim       Biology       78000         58763       Crick       Elec. Eng.       80000         52187       Mozart       History       65000         32343       El Said       History       86000  |   | 21212 | Wu       | Finance    | 90000  |
| 98531         Kim         Biology         78000           58763         Crick         Elec. Eng.         80000           52187         Mozart         History         65000           32343         El Said         History         86000  |   | 10101 | Brandt   | Comp. Sci. | 82000  |
| 58763         Crick         Elec. Eng.         80000           52187         Mozart         History         65000           32343         El Said         History         86000  |   | 43521 | Katz     | Comp. Sci. | 75000  |
| 52187MozartHistory6500032343El SaidHistory86000  |   | 98531 | Kim      | Biology    | 78000  |
| 32343 El Said History 86000  |   | 58763 | Crick    | Elec. Eng. | 80000  |
| 32343 El Said History 86000  |   | 52187 | Mozart   | History    | 65000  |
| y  | у | 32343 | El Said  | History    | 86000  |

The query result

| dept_name  | avg_salary |
|------------|------------|
| Physics    | 91000      |
| Finance    | 90000      |
| Comp. Sci. | 78500      |
| Biology    | 78000      |
| Elec. Eng. | 80000      |
| History    | 75500      |



#### **Aggregate Functions (Cont.)**

 Find the average salary of instructors in each department which has average salary greater than 80000 – use HAVING because WHERE cannot be used with aggregate functions

SELECT dept\_name, AVG (salary) AS avg\_salary FROM instructor GROUP BY dept\_name

HAVING avg\_salary > 80000;

| The query result |  |  |  |
|------------------|--|--|--|
| avg_salary       |  |  |  |
| Physics 91000    |  |  |  |
| Finance 90000    |  |  |  |
|                  |  |  |  |

| ID    | name     | dept_name  | salary |
|-------|----------|------------|--------|
| 22322 | Einstein | Physics    | 95000  |
| 33452 | Gold     | Physics    | 87000  |
| 21212 | Wu       | Finance    | 90000  |
| 10101 | Brandt   | Comp. Sci. | 82000  |
| 43521 | Katz     | Comp. Sci. | 75000  |
| 98531 | Kim      | Biology    | 78000  |
| 58763 | Crick    | Elec. Eng. | 80000  |
| 52187 | Mozart   | History    | 65000  |
| 32343 | El Said  | History    | 86000  |



# **Subqueries**

- SQL provides a mechanism for the nesting of subqueries.
- A **subquery** is a **SELECT-FROM-WHERE** expression that is nested within another query.
- The nesting can be done in the following SQL query

```
SELECT A_1, A_2, \dots, A_n
FROM r_1, r_2, \dots, r_n
WHERE P
```

as follows:

- $A_i$  can be replaced be a subquery that generates a single value.
- $r_i$  can be replaced by any valid subquery
- *P* can be replaced with an expression of the form:
  - B < operation > (subquery)



### **Subqueries – Examples (Subquery in the WHERE clause)**

 Find courses offered in Fall 2009 and in Spring 2010 SELECT DISTINCT course\_id FROM section WHERE semester = 'Fall' AND year = 2009 AND course\_id IN (SELECT course\_id FROM section

WHERE semester = 'Spring' AND year= 2010);



# **Subqueries – Examples (Subquery in the FROM clause)**

• Find the average instructors' salaries of those departments where the average salary is greater than \$42,000."



# **Subqueries – Examples (Subquery in the SELECT clause)**

• List all departments along with the number of instructors in each department

```
SELECT dept_name,
 (SELECT COUNT(*)
 FROM instructor
 WHERE department.dept_name = instructor.dept_name)
 AS num_instructors
FROM department;
```

- Runtime error if subquery returns more than one result tuple
- Note that: subqueries are parenthesized SELECT-FROM-WHERE statements





# Wrap-Up

 Summarize what you learned today in 2minutes



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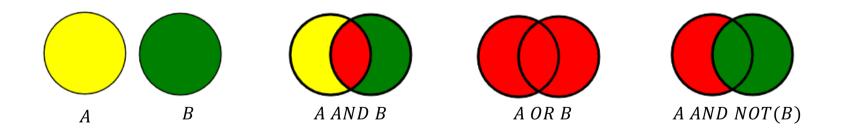
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**Boolean Operators – Revision** 



#### **Boolean Operators**

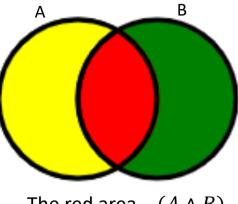
- Searching through a database or search engine can often be frustrating
- Boolean Operators create relationships between concepts and terms for better search results
- Most popular Boolean operators are AND, OR and NOT
  - The red areas represent the results of the operators





# AND $(\Lambda)$

| A | B | $A \wedge B$ |
|---|---|--------------|
| 1 | 1 | 1            |
| 1 | 0 | 0            |
| 0 | 1 | 0            |
| 0 | 0 | 0            |



The red area –  $(A \land B)$ 

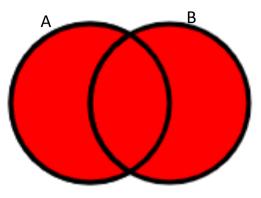
- Retrieves only records that satisfy both conditions
- Example:

name = "Taylor" AND dept\_name = "Chem." Returns all instructors in the Chem. department whose name is Taylor



# OR(V)

| A | B | $A \lor B$ |
|---|---|------------|
| 1 | 1 | 1          |
| 1 | 0 | 1          |
| 0 | 1 | 1          |
| 0 | 0 | 0          |



The red area –  $(A \lor B)$ 

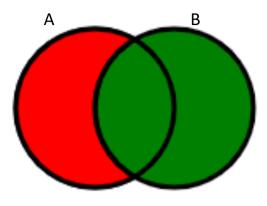
- Retrieves records that satisfy one of the conditions
- Example:

name = "Taylor" OR dept\_name = "Chem." Returns all instructors with the name Taylor and all instructors of the Chem. department



# NOT (~)

| A | ~ <i>A</i> |
|---|------------|
| 1 | 0          |
| 0 | 1          |



The red area -A AND NOT(B)

- Retrieves only records that satisfy the first condition and doesn't satisfy the second
- Example:

name = "Taylor" AND NOT dept\_name = "Chem." Returns all instructors with the name Taylor who do not work in the Chem. department



#### **Boolean Equivalence**

- Equivalence of two Boolean operations can be easily proven using truth tables
- Equivalence of Boolean operations is useful for optimizing the Boolean queries
- Examples:

• ~ 
$$(A \land B) \equiv ~ A \lor ~ B \longrightarrow$$

- $(A \land B) \land \sim B \equiv A \land (B \land \sim B) \equiv false$
- $(A \land B) \lor (\sim B \land C) \lor (A \land C) \lor \sim (A \land C) \equiv (A \land C) \lor \sim (A \land C) \equiv true$



### **Proving Boolean Equivalence**

- Truth Table: Helpful when the number of statements in the Boolean expression is small
- Proof by contradiction: assume the expression is false/true and proof that it leads to contradiction
- Using the Boolean axioms.



- Let *T* and *F* represent the cases of always True and always False
  - $(T \wedge T) = T$
  - $(F \wedge F) = F$
  - $(T \lor T) = T$
  - $(F \lor F) = F$
  - $(T \wedge F) = (F \wedge T) = F$
  - $(T \lor F) = (F \lor T) = T$

• 
$$\overline{T} = F$$

• 
$$\overline{F} = T$$



- Commutativity
  - $(A \land B) = (B \land A)$
  - $(A \lor B) = (B \lor A)$
- Identity
  - $(A \wedge T) = A$
  - $(A \lor T) = T$
  - $(A \wedge F) = F$
  - $(A \lor F) = A$



- Idempotent
  - $(A \land A) = A$
  - $(A \lor A) = A$
- Involution
  - $\overline{\overline{A}} = A$
- Complement
  - $(A \wedge \overline{A}) = F$
  - $(A \lor \overline{A}) = T$



- Associativity
  - $(A \land B) \land C = A \land (B \land C)$
  - $(A \lor B) \lor C = A \lor (B \lor C)$
- Distributivity
  - $A \land (B \lor C) = (A \land B) \lor (A \land C)$
  - $A \lor (B \land C) = (A \lor B) \land (A \lor C)$



#### **Proving Boolean Equivalence**

- Using the Boolean axioms (Example):
  - prove that:  $(A \land B) \lor (\sim A \land C) \lor (B \land C) = (A \land B) \lor (\sim A \land C)$

• T means always TRUE.



Read more FROM John Kelly, The Essence of Logic (Prentice Hall, 1997) Chapter 1 is good enough

